



π IN THE SKY⁸

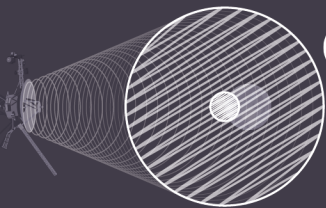
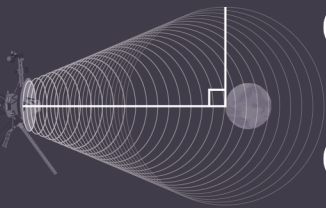
Answer Key

Signal Solution

What fraction of Voyager's original signal is received by a 70 meter antenna on Earth?

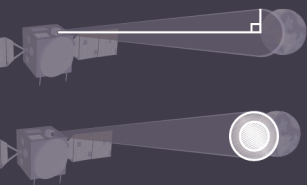


- Convert astronomical units to meters.
 $124 \text{ AU} \cdot (150,000,000 \text{ km} / 1 \text{ AU}) \cdot (1,000 \text{ m} / 1 \text{ km}) = 1.86 \cdot 10^{13} \text{ m}$
- Find the beam radius at Earth using tangent and the distance between Earth and Voyager.
 $\tan 0.25^\circ \approx x / (1.86 \cdot 10^{13} \text{ m}) \rightarrow 8.12 \cdot 10^{10} \text{ m}$
- Find the ratio of the antenna area (radius of 35 m) to the signal area.
 $\pi(35 \text{ m})^2 / \pi(8.12 \cdot 10^{10} \text{ m})^2 \approx 1.9 \cdot 10^{-19}$
- Find the ratio of received signal versus the sent signal.
 $1.9 \cdot 10^{-19} \cdot 12.5 \text{ W} \approx 2.3 \cdot 10^{-18} \text{ W or } 1.8 \cdot 10^{-20} \%$



What fraction of the signal from a DSOC-equipped spacecraft is received?

- Follow the same process as above with the values for the DSOC-equipped spacecraft.
 $24 \text{ AU} \cdot (150,000,000 \text{ km} / 1 \text{ AU}) \cdot (1,000 \text{ m} / 1 \text{ km}) \approx 1.86 \cdot 10^{13} \text{ m}$
 $\tan 0.00045^\circ \approx x / (1.86 \cdot 10^{13} \text{ m}) \rightarrow 1.46 \cdot 10^8 \text{ m}$
 $\pi(35 \text{ m})^2 / \pi(1.46 \cdot 10^8 \text{ m})^2 \approx 5.7 \cdot 10^{-14}$
 $5.7 \cdot 10^{-14} \cdot 4 \text{ W} \approx 2.3 \cdot 10^{-13} \text{ W or } 5.8 \cdot 10^{-14} \%$



By what factor is DSOC more effective?

- Divide the received wattage of the DSOC spacecraft's signal by that of Voyager's.
 $2.3 \cdot 10^{-13} / 2.3 \cdot 10^{-18} = 10^5 \text{ or } 100,000 \text{ times more effective}$

